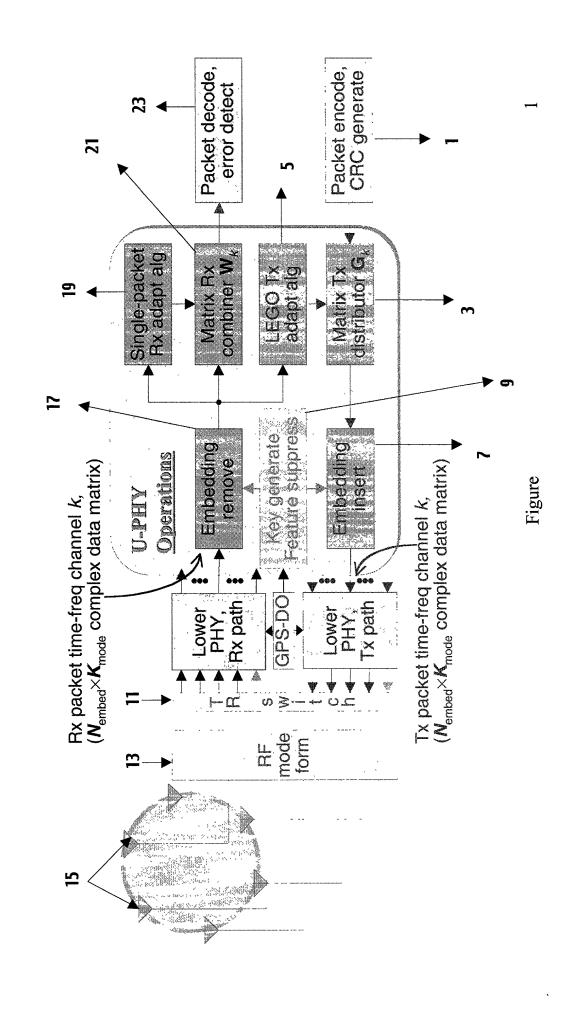
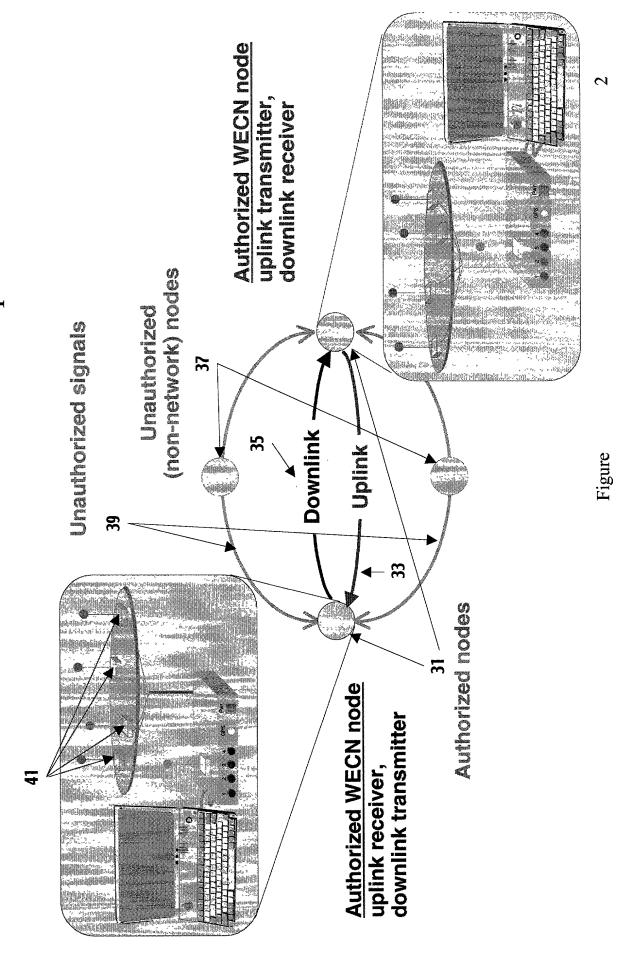
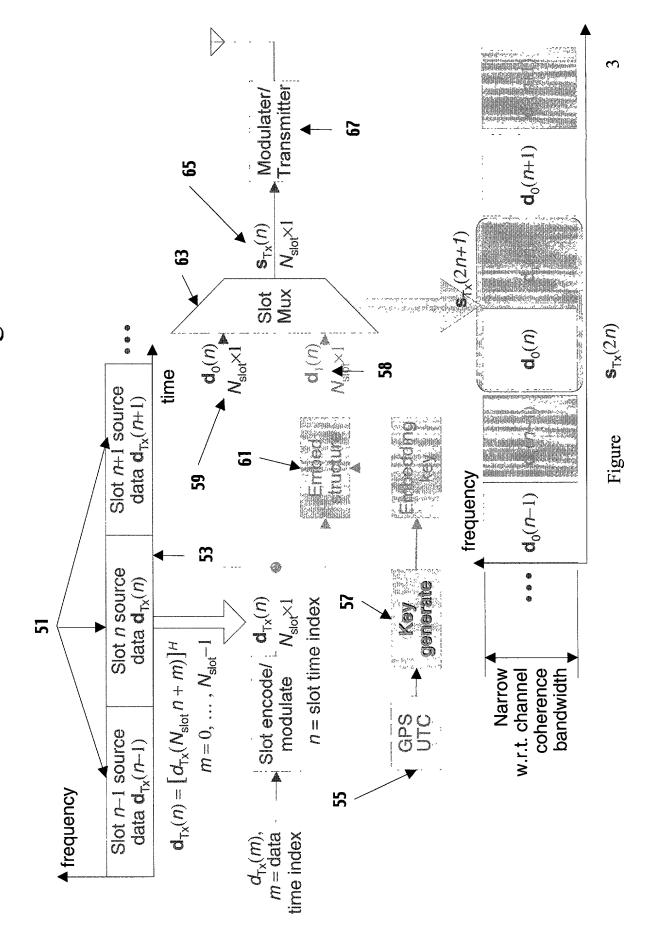
# WECN Structural Embedding/Removal

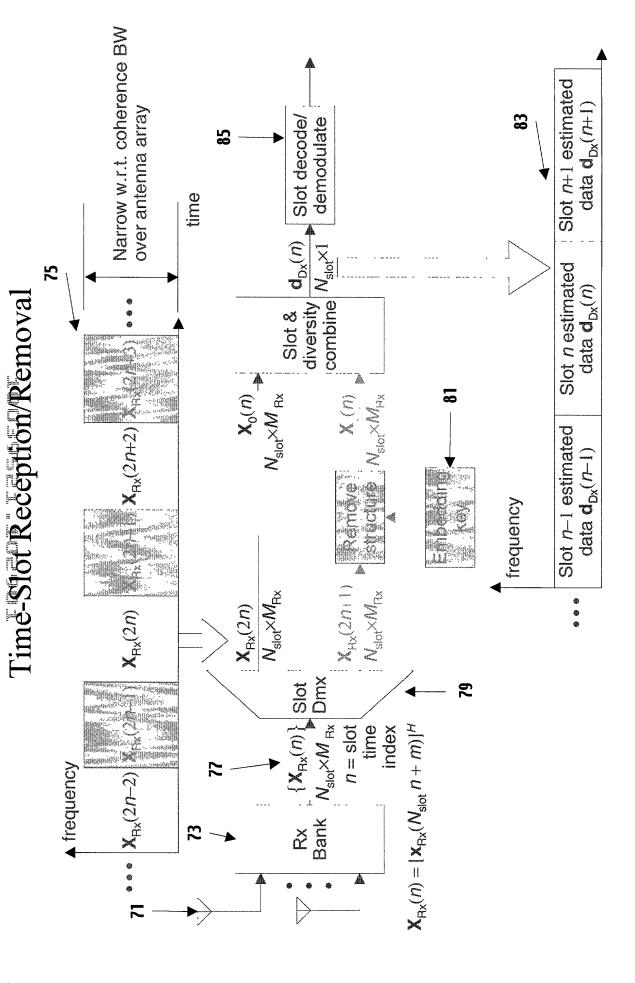


## WECN with external sources/recipients



### Time-Slot Embedding

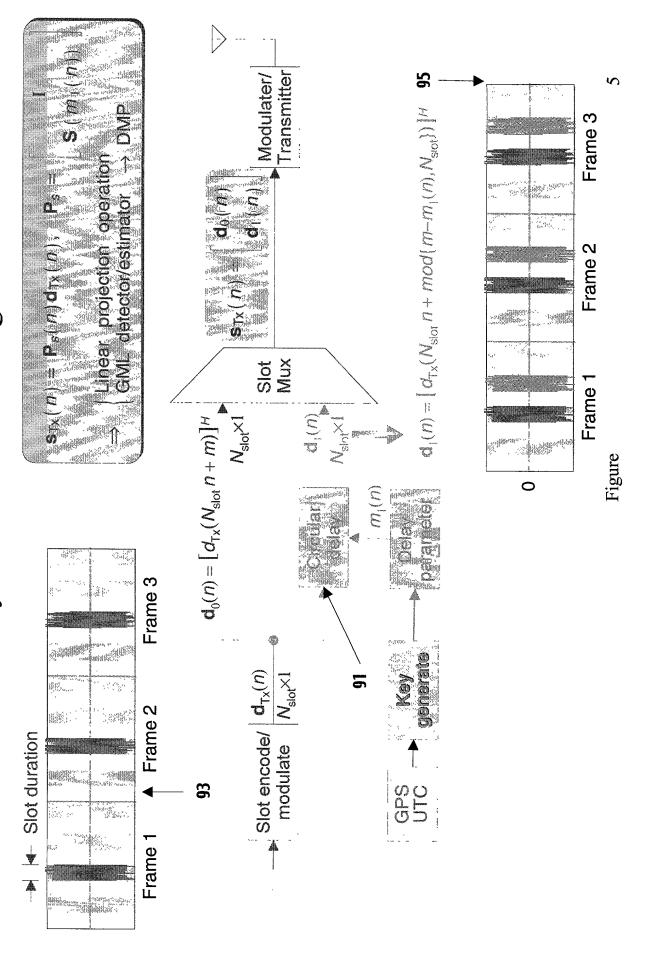




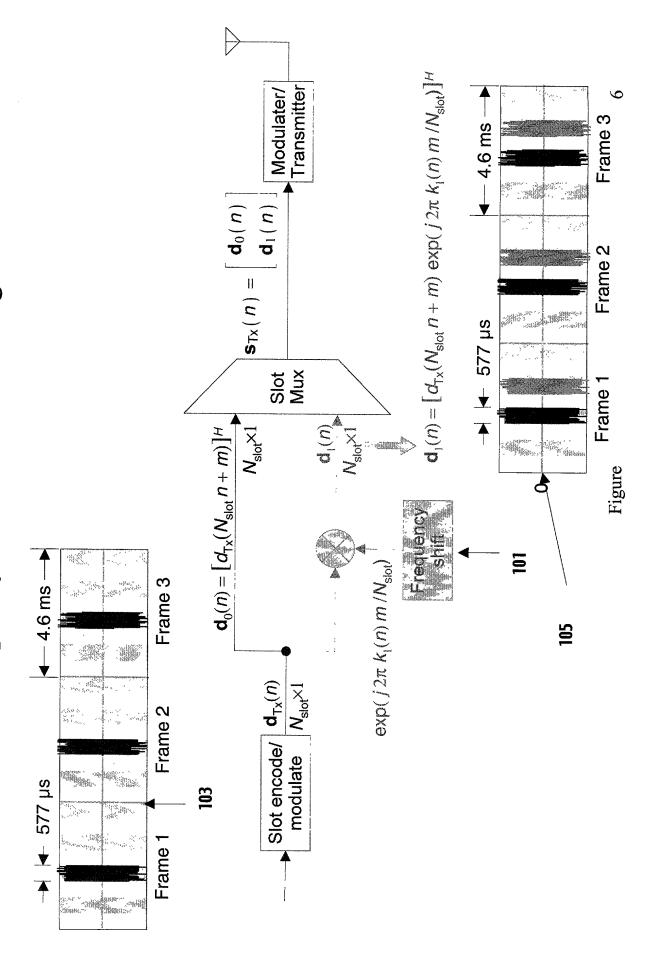
Figure

7

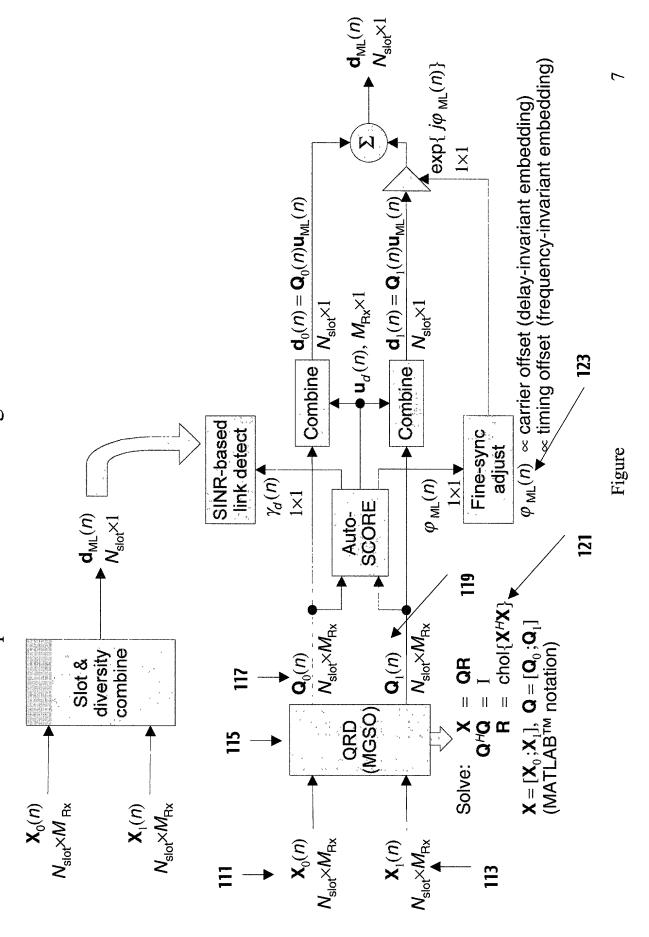
### Delay-Invariant Embedding



### Frequency-Invariant Embedding



Auto-SCORE Adaptation - Data whitening & environmental evaluation



# Single-Link Auto-SCORE Algorithm - Software

Combine  $N_t \times M$  matrices  $X_0$  and  $X_1$  into single  $2N \times M$  matrix X.

$$\mathbf{X} = [\mathbf{X}_0^H \ \mathbf{X}_1^H]^H$$

where  $N = N_{\text{slot}} M = M_{\text{Rx}}$  if time-slot embedding is employed at the transmitter. Compute **QR** decomposition of X,

$$X = QR$$

$$I = O_{H}$$

$$\mathbf{Q}^H \mathbf{Q} = \mathbf{I}$$

$$\mathbf{R} = \operatorname{chol}\{\mathbf{X}^H \mathbf{X}\},\,$$

where Q is defined by

$$\mathbf{Q} = [\mathbf{q}_1 \dots \mathbf{q}_M]$$
$$= [\mathbf{q}(1) \dots \mathbf{q}(N)]^H$$

Separate Q into  $N \times M$  submatrices  $Q_0$  and  $Q_1$ , such that

$$X = X_0$$

$$\mathbf{Q}_0 = \mathbf{X}_0 \mathbf{C}$$
$$\mathbf{Q}_1 = \mathbf{X}_1 \mathbf{C},$$

where  $C = \mathbb{R}^{-1}$ . Form  $M \times M$  cross-correlation matrix S,

$$\mathbf{S} = (1/N) \, \mathbf{Q}_0^H \mathbf{Q}_1.$$

Initialize whitened linear combiner weights

$$\mathbf{u} = [s(m,M)]$$

$$v = \|\mathbf{u}\| (L_2 \text{ norm})$$

$$\mathbf{u} \leftarrow \mathbf{u}/v$$

$$\lambda/n \rightarrow n$$

Iteratively update combiner weights (preset iterations, or until stopping criterion met)

$$\mathbf{v} = \mathbf{S}\mathbf{u}$$

$$\rho = 1/2 \operatorname{sign} \{\mathbf{v}^H \mathbf{u}\}$$

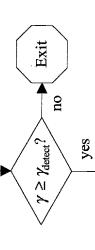
$$\mathbf{u} \leftarrow \rho \mathbf{v} + \rho^* \mathbf{S}^H \mathbf{u}$$

$$\mathbf{v} = \|\mathbf{u}\| \ (\mathbf{L}_2 \text{ norm})$$

$$r = \|\mathbf{u}\| (\mathbf{L}_2 \text{ norm})$$

Compute output SINR measurement  $\chi$ 

$$\gamma = \nu/(1-\nu)$$



Compute phase-shift estimate  $\phi$ ,

Compute slot/diversity combined output data

$$= \mathbf{Q}_0 \mathbf{u} + (\mathbf{Q}_1 \mathbf{u}) e^{-j\varphi}$$

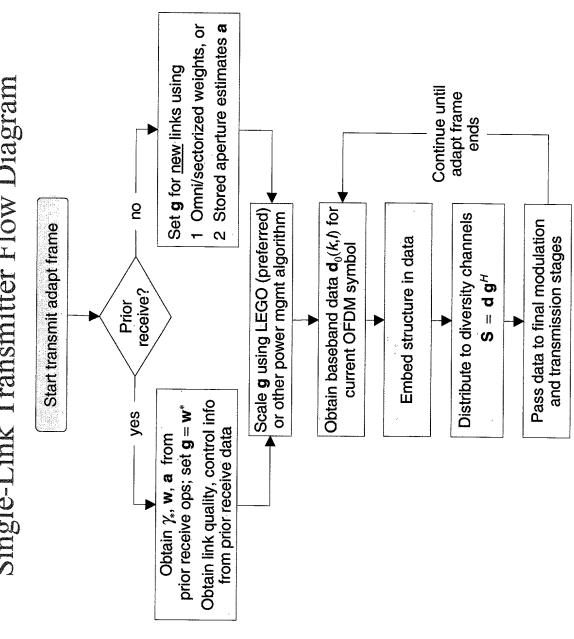
Compute unwhitened combiner weights w, aperture vector a,

$$\mathbf{w} = \mathbf{C}\mathbf{u}$$

$$\mathbf{a} = \mathbf{R}^H \mathbf{u}$$

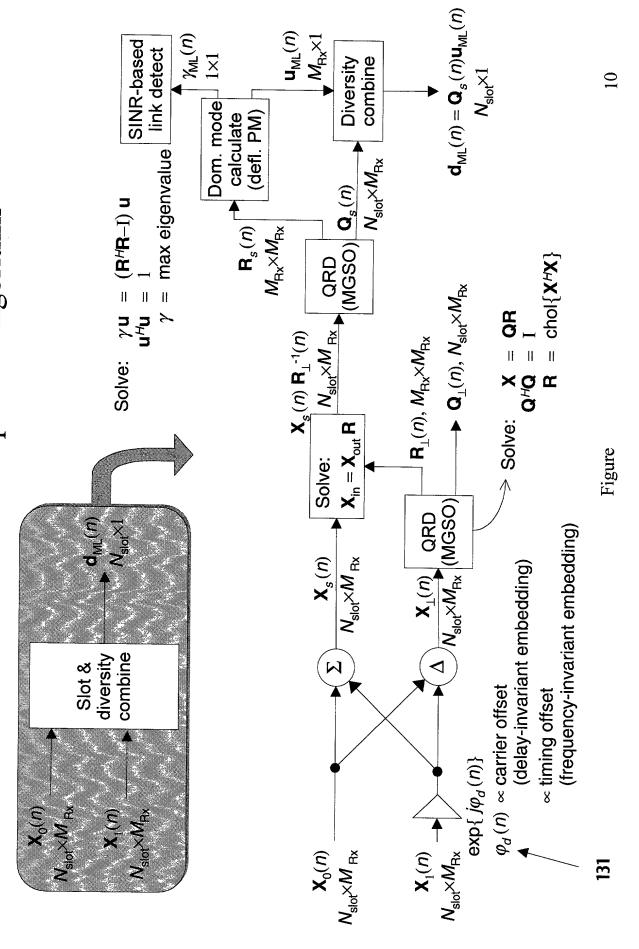
Figure

## Single-Link Transmitter Flow Diagram



Figure

# Alternative DMP Adaptation Algorithm



### alternative converging embedded-signal-differentiation algorithms

#### Dominant-Mode Prediction

 $\gamma \mathbf{u} = (\mathbf{R}^H \mathbf{R} - \mathbf{I}) \mathbf{u}$   $\|\mathbf{u}\| = 1 (\mathbf{L}_2 \text{ norm})$   $\gamma = \text{max eigenvalue}$ Solve:

#### **Optimization Algorithm**

Initialize:  $\mathbf{u} = r(M,M) [r^*(M,1) - 1]$   $\gamma = ||\mathbf{u}|| (L_2 \text{ norm})$ 

lterate:

#### Auto-SCORE

SON SON

 $V(\phi) \mathbf{u} = \mathbf{S}(\phi) \mathbf{u}$   $\mathbf{S}(\phi) = 1/2(\mathbf{S}\Theta^{\dagger \phi} + \mathbf{S}^H\Theta^{-\dagger \phi})$   $||\mathbf{u}|| = 1 \ (\mathbf{L}_2 \text{ norm})$ 

 $v(\phi) = \max \text{ eigenvalue}$ 

 $\varphi = \arg \max_{\varphi} v(\varphi)$ 

#### Optimization Algorithm

Initialize;

 $\mathbf{u} = [s(m, M)]$  $v = ||\mathbf{u}|| \ (L_2 \text{ norm})$ 

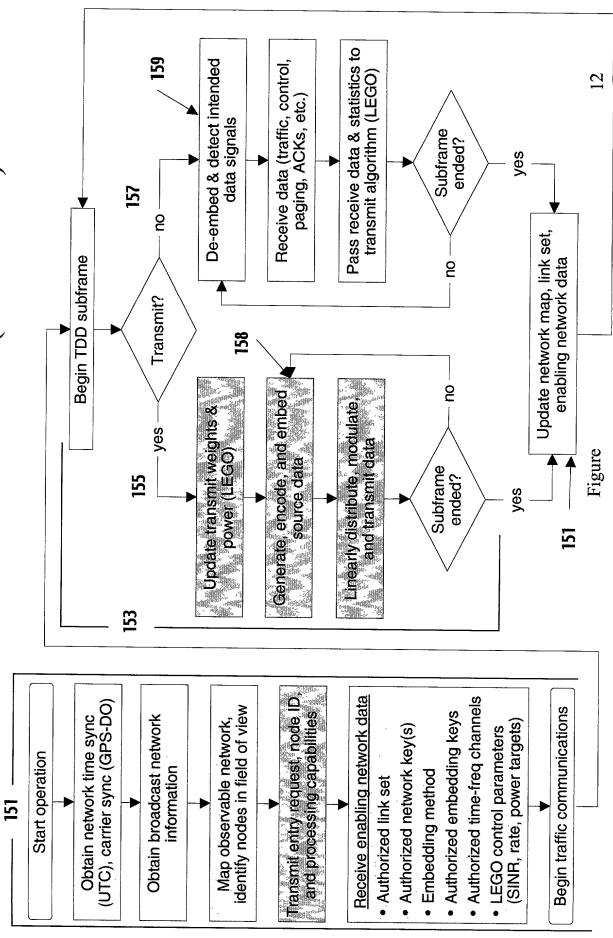
 $\rho = 1/2 \operatorname{sign}\{\mathbf{v}^{H}\mathbf{u}$ 

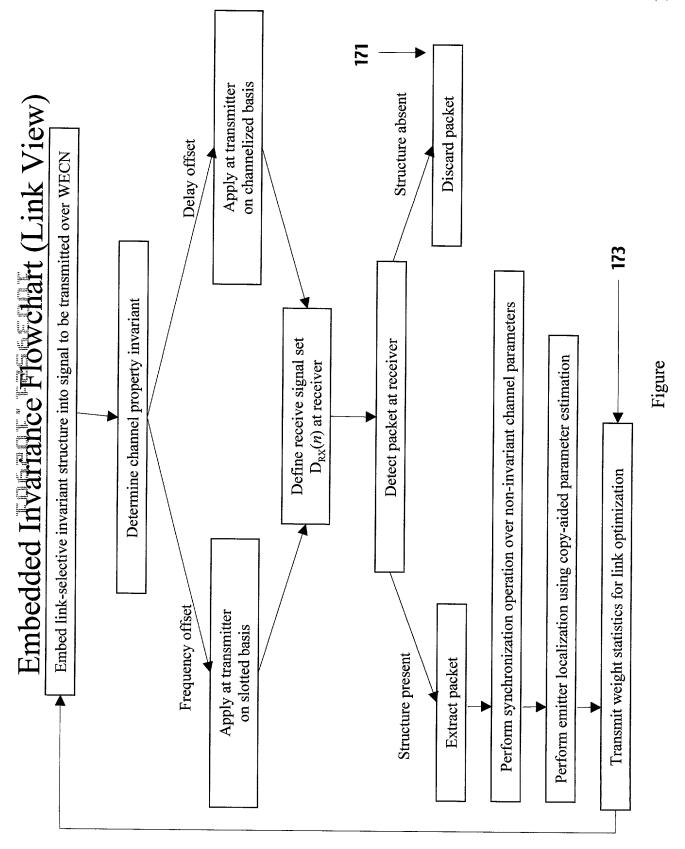
Finalize:

 $\gamma = v/(1-v)$ 

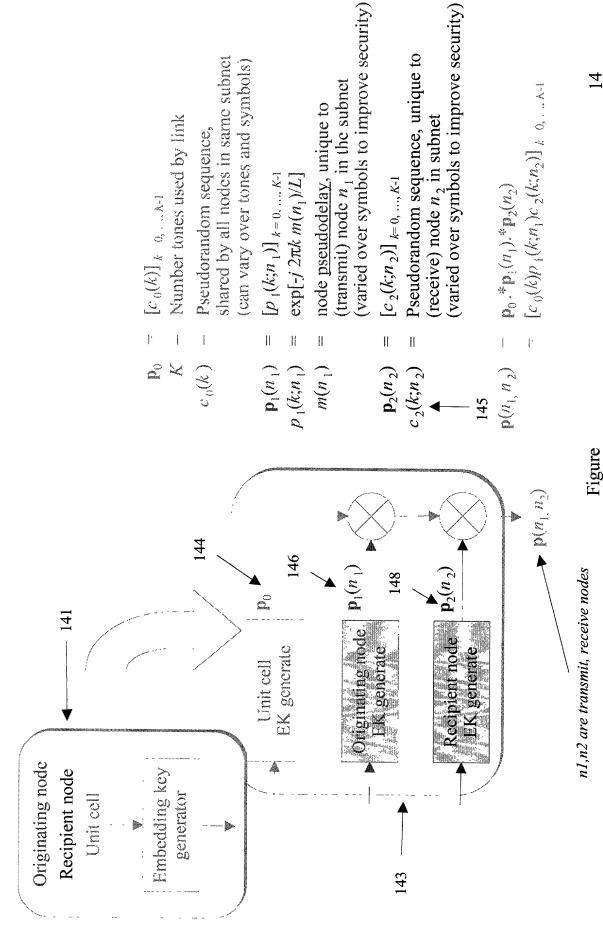
Figure

Embedded Invariance Flowchart (Nodal View)



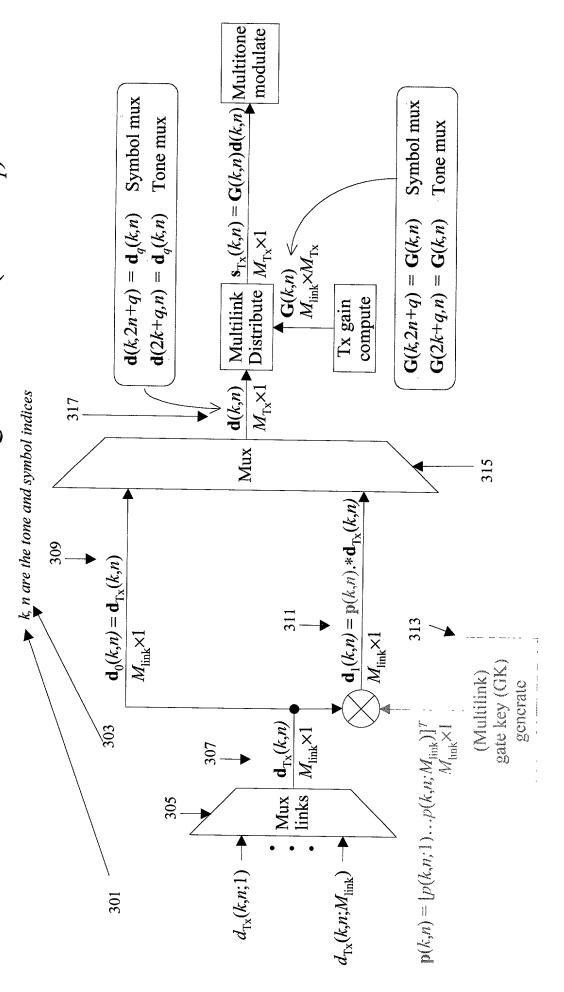


# Multilink Embedding Key Generation Algorithm

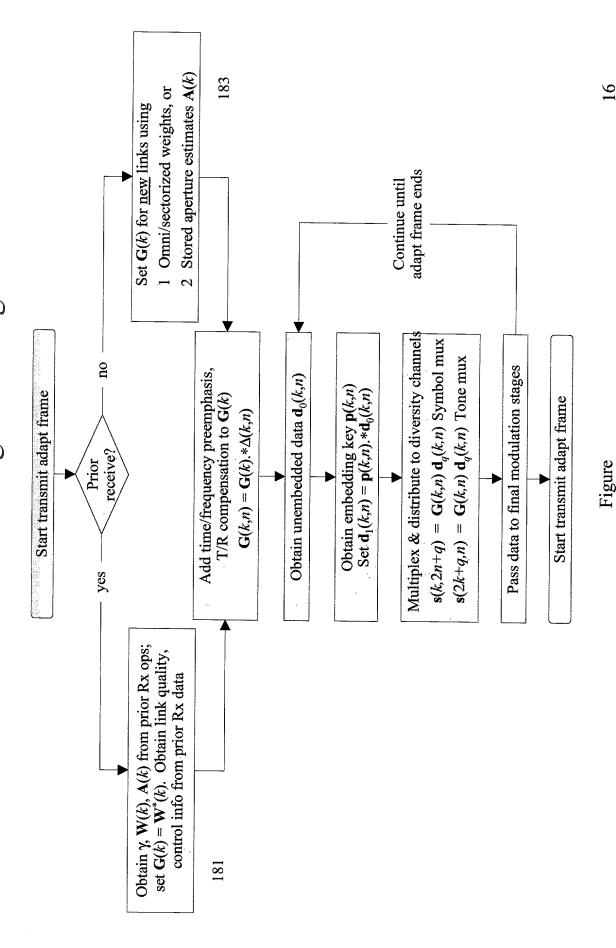


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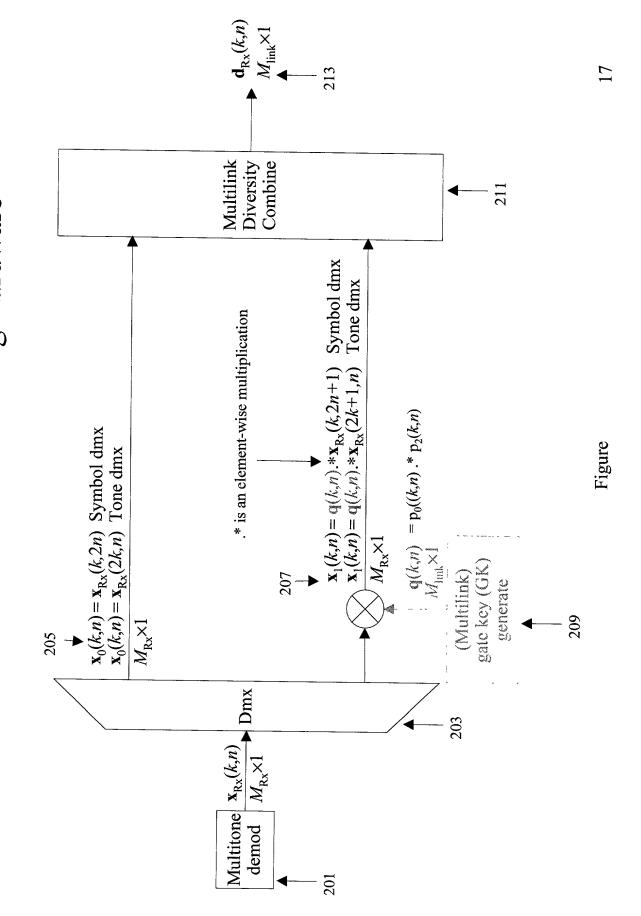
### Multilink Transmit Embedding Hardware (Node $n_1$ )



Figure



Multilink Receive Embedding Hardware 



### Multilink Receiver Flow Diagram

Start receive adapt frame

Obtain data from  $x_{Rx}(k,n)$  tone dmx of current OFDM symbol Obtain partial code  $\mathbf{q}(k,n) = [\mathbf{p}_0(k,n).*\mathbf{p}_1(k,n)]^*$ 

Demux  $\mathbf{x}_{Rx}(k,n)$  into  $\mathbf{x}_0(k,n)$  and  $\mathbf{x}_1(k,n)$ 

$$\mathbf{x}_0(k,n) = \mathbf{x}_{\mathrm{Rx}}(k,2n)$$
  
 $\mathbf{x}_0(k,n) = \mathbf{x}_{\mathrm{Rx}}(2k,n)$ 

$$\eta = \mathbf{x}_{\text{Rx}}(2k,n)$$

$$\mathbf{x}_1(k,n) = q(k,n).*\mathbf{x}_{\mathrm{Rx}}(k,2n+1)$$
 Symbol dmx  $\mathbf{x}_1(k,n) = q(k,n).*\mathbf{x}_{\mathrm{Rx}}(2k+1,n)$  Tone dmx

Combine into submatrices  $X_0(n)$ ,  $X_1(n)$ 

$$\mathbf{X}_0(n) = [\mathbf{x}_0(1,n) \dots \mathbf{x}_0(K,n)]^H$$

$$\mathbf{X}_1(n) = [\mathbf{x}_1(1,n) \dots \dot{\mathbf{x}}_1(K,n)]^H$$

Combine  $K \times M$  matrices  $X_0(n)$  and  $X_1(n)$ , into single  $2K \times M$  matrix X,

$$\mathbf{X} = \left[ \mathbf{X}_0^H(n) \mathbf{X}_1^H(n) \right]^H$$

where  $N = N_{\text{stor}}$ ,  $M = M_{\text{Rx}}$  if time-slot embedding is employed at the transmitter.

Compute **QR** decomposition of X, X = QR

Separate Q into  $N \times M$  submatrices  $Q_0$  and  $Q_1$ , such that

$$\mathbf{Q}_0 = \mathbf{X}_0 \mathbf{C}$$

$$\mathbf{Q}_1 = \mathbf{X}_1 \mathbf{C},$$

where  $C = \mathbb{R}^{-1}$ . Form  $M \times M$  cross-correlation matrix S,

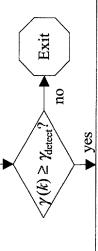
$$\mathbf{S} = (1/N) \mathbf{Q}_0^H \mathbf{Q}_1$$

Continue until adapt frame Form  $M \times M$  cross-correlation matrix S(m),

 $\mathbf{S} = \text{IFFT}_K \{ \mathbf{q}_0(k) \, \mathbf{q}_1^H(k) \}$ 

over possible pseudodelays 
$$\tau(m)=mT_{\text{sample}}$$
.

Calculate modified auto-SCORE eigenvalues  $\{\chi(m), \mathbf{u}(m), \varphi(m) \text{ over valid pseudodelays.}$ 



#### Compute:

Number received signals Qlink

Observed pseudodelays and phase shift  $\mathbf{m}_* = [m_*(1) \dots m_*(Q_{\text{link}})]$ 

$$\rho_* = \exp(i\phi(\mathbf{m}_*))$$

Combiner weights U

$$\mathbf{U}_* = \mathbf{U}(\mathbf{m}_*)$$

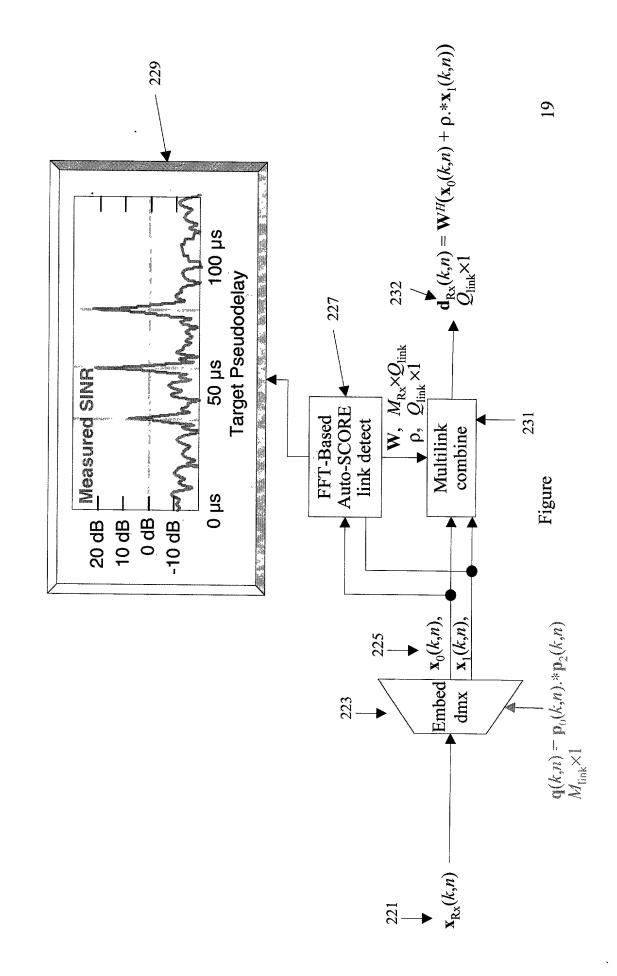
Estimate extraction SINR

$$\gamma_* = \gamma(\mathbf{m}_*)$$
Received data

 $\mathbf{D}_* = (\mathbf{Q}_0 + \mathbf{Q}_1 \operatorname{diag}\{\mathbf{p}_*\})\mathbf{U},$ 

Figure

### Link Detection, Separation Operation



Pseudodelay Plots and Antenna Patterns

